

Task 7 proof

Long $f(\text{int } n)$ can be written as:

$$f(n) = \begin{cases} 0, & n=0 \\ -f(n), & n < 0 \\ f(n-1) + 3n \cdot (n-1), & n > 0 \end{cases}$$

Let's test $f(4)$:

$$\begin{aligned} f(4) &= f(3) + 3 \cdot 4 \cdot (4-1) \\ f(3) &= f(2) + 3 \cdot 3 \cdot (3-1) \\ f(2) &= f(1) + 3 \cdot 2 \cdot (2-1) \\ f(1) &= f(0) + 3 \cdot 1 \cdot (1-1) \\ f(0) &= 0 \end{aligned}$$

We can see that any $f(n)$ would sum up all $f(n)$ ^{from 0} up to n this can be written as:

$$\sum_{n=1}^n 3n(n-1)$$

If we multiply we get: $\sum_{n=1}^n 3n^2 - 3n$

The full function becomes:

$$f(n) = \begin{cases} 0, & n=0 \\ -\sum_{n=1}^n 3n^2 + 3n, & n < 0 \\ \sum_{n=1}^n 3n^2 - 3n, & n > 0 \end{cases}$$

$$\text{Since } \sum_{n=0}^{\infty} 3n^2 + 3n = 0 \text{ and } -\sum_{n=0}^{\infty} 3n^2 + 3n =$$

$$\sum_{n=0}^{\infty} 3n^2 - 3n$$

We can simplify to:

$$f(n) = \sum_{n=0}^{\infty} 3n^2 + 3n$$

When implementing this in C++ I used ~~the~~ a if statement to make the negative input loop a positive number of times:

```
//My implementation:
long f2(int n)
{
    long result = 0;
    if(n < 0)
    {
        for (long i = 0; i <= n * -1; i++)
        {
            result += -(3 * i * i - 3 * i);
        }
    }
    else
    {
        for (long i = 0; i <= n; i++)
        {
            result += 3 * i * i - 3 * i;
        }
    }
    return result;
}
```